

# Statistical Properties of Electromagnetic Environment in Wireless Networks, Intra-Network Electromagnetic Compatibility and Safety

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**Abstract**—Statistical properties of electromagnetic environment in wireless networks affecting its intra-network electromagnetic compatibility and safety are studied. The analysis is based on the standard propagation channel model, a Poisson model of random spatial distribution of transmitters, and a threshold-based model of the victim receptor behaviour (radio receiver or human body). The distribution of dominant interference level is derived and analysed under various network and system configurations. The aggregate interference is dominated by the nearest transmitter one. The distribution of the unordered single-node interference is independent of the transmitters' power and their spatial density and is the same for homogeneous and non-homogeneous networks. The outage probability is used as a measure of not only the wireless link quality-of-service, but also of environmental risks induced by electromagnetic radiation. The maximum acceptable interference levels for reliable link performance and for low environmental risks are surprisingly similar.

*Keywords*-electromagnetic environment, dynamic range, outage probability, wireless networks

## I. INTRODUCTION

Electromagnetic compatibility (EMC) and safety (EMS) of wireless communication networks have been recently a subject of extensive studies. Mutual interference among several links (e.g. several users) operating at the same time places a fundamental limit to the network performance and also determines the level of electromagnetic environmental risks to the population. The effect of interference in wireless networks at the physical layer has been studied from several perspectives [1]-[5]. A typical statistical model of interference in a network includes a model of spatial location of the nodes, a propagation path loss law (which includes the average path loss and, possibly, large-scale (shadowing) and small-scale (multipath) fading) and a threshold-based receiver performance model. The most popular choice for the model of the node spatial distribution is Poisson point process on a plane [1]-[5]. Based on this model and ignoring the effect of fading, Sousa [2] has obtained the characteristic function (CF) of the aggregate (total) interference at the receiver, which can be transformed into a closed-form probability density function (PDF) in some special cases, and, based on it, the error rates for direct sequence and frequency hopping systems. While

using the LePage series representation, Ilow and Hatzinakos [3] have developed a generic technique to obtain the CF of aggregate interference from a Poisson point process on a plane (2-D) and in a volume (3-D), which can be used to incorporate the effects of Rayleigh and log-normal fading in a straightforward way. Relying on a homogeneous Poisson point process on a plane, Weber et al [4] have characterized the transmission capacity of the network subject to the outage probability constraint via lower and upper bounds. In a recent work, Weber et al [5] use the same approach to characterize the network transmission capacity when the receivers are able to suppress some powerful interferers.

A common feature of all these works is the use of aggregate interference (either alone or in the form of signal-to-interference-plus-noise ratio), and a common lesson is that it is very difficult to deal with: while the CF of aggregate interference can be obtained in a closed form, the PDF or CDF are available only in a few special cases. This limits significantly the amount of insight that can be extracted from such a model, especially if no approximations or bounds are used.

To overcome this difficulty, we adopt a different approach: instead of relying on the aggregate interference power as a performance indicator, we use the power of the dominating interfering signal [7]-[11]. While this is clearly an approximation, closed-form performance evaluation becomes feasible and significant insight can be extracted from such a model. Furthermore, since the aggregate interference is dominated by the most powerful interferer in the region of low outage probability (i.e. the practically-important region), both models give roughly the same results (see [11] for details). This observation is also consistent with the corresponding results in [4][5], when the “near-field” region contains only one interferer. Thus, in the framework of [4][5], our results represent the (tight) lower bound on the outage probability.

Using this model, we study the power distribution of the ensemble of interferences and the dominant interferer in various scenarios, which is further used to obtain compact closed-form expressions for the outage probability of a given receptor (or, equivalently, of the link of a given user) in the 1-

D, 2-D and 3-D Poisson field of interferers, for both uniform and non-uniform average node densities and for various values of the average path loss exponent. Comparison to the corresponding results in [2] (obtained in terms of the error rates) indicates that the dominant contribution to the error rate is due to the outage events caused by the closest (i.e. dominant) interferer, which increases with the average node density. The proposed method is flexible enough to include the case when a given number of strongest interferers are suppressed. The outage probability is shown to scale down exponentially in this number. Contrary to [5], we do not rely in this case on the simplifying assumption of canceling *all* interferers in the disk with the given average number of interferers; neither we assume that only interferers more powerful than the required signal are cancelled (the last assumption affects significantly the result), i.e. our analysis of interference cancellation is exact. The proposed method can also be used to include the effect of fading. We argue that Rayleigh fading has a negligible effect on the distribution of dominant interferer's power and the effect of log-normal fading (shadowing) is to shift the distribution by a constant non-negligible factor [11].

Our analysis culminates in the formulation of the outage probability-network density tradeoff: for a given average density of the nodes, the outage probability is lower bounded or, equivalently, for a given outage probability, the average density of the nodes is upper bounded. This tradeoff is a result of the interplay between a random geometry of node locations, the propagation path loss and the distortion effects at the victim receiver. Our analysis is based on the framework originally developed in [7]-[11].

We argue that the outage probability, which is traditionally used as a measure of quality-of-service in wireless systems and networks, also measures the environmental risks to the population induced by electromagnetic radiation of wireless devices.

The paper is organized as follows. In Section 2, we introduce the system and network model. In Section 3, the distribution of interference levels and of the dynamic range (dominant interference-to-noise ratio) is given for this model. Based on this, the node density – outage probability tradeoff is presented in Section 4. The maximum acceptable interference levels for high quality-of-service wireless network performance and for low electromagnetic environmental risks to the population are shown to be surprisingly similar in Section 5.

## II. NETWORK AND SYSTEM MODEL

As an interference model of wireless network at the physical layer, we consider a number of point-like transmitters (Tx) and receptors (Rx) that are randomly located over a certain limited region of space  $S_m$ , which can be one ( $m = 1$ ), two ( $m = 2$ ), or three ( $m = 3$ ) -dimensional (1-D, 2-D or 3-D). This can model location of the nodes over a highway or a street canyon (1-D), a residential area (2-D), or a downtown area with a number of high-rise buildings (3-D). In our analysis, we consider a single (randomly-chosen) receiver (or some other receptor which is susceptible to electromagnetic

fields generated by transmitters) and a number of transmitters that generate interference to this receiver. We assume that the spatial distribution of the transmitters (nodes) has the following properties: (i) for any two non-overlapping regions of space  $S_a$  and  $S_b$ , the probability of any number of transmitters falling into  $S_a$  is independent of how many transmitters fall into  $S_b$ , i.e. non-overlapping regions of space are statistically independent; (ii) for infinitesimally small region of space  $dS$ , the probability  $\mathcal{P}(k=1, dS)$  of a single transmitter ( $k=1$ ) falling into  $dS$  is  $\mathcal{P}(k=1, dS) = \rho dS$ , where  $\rho$  is the average spatial density of transmitters (which can be a function of position). The probability of more than one transmitter falling into  $dS$  is negligible,  $\mathcal{P}(k > 1, dS) \ll \mathcal{P}(k=1, dS)$  as  $dS \rightarrow 0$ . Under these assumptions, the probability of exactly  $k$  transmitters falling into the region  $S$  is given by Poisson distribution,

$$\mathcal{P}(k, S) = e^{-\bar{N}} \bar{N}^k / k!, \quad \bar{N} = \int_S \rho dS \quad (1)$$

where  $\bar{N}$  is the average number of transmitters falling into the region  $S$ . If the density is constant, then  $\bar{N} = \rho S$ . Possible scenarios to which the assumptions above apply, with a certain degree of approximation, are a sensor network with randomly-located non-cooperating sensors; a network(s) of mobile phones from the same or different providers (in the same area); a network of multi-standard wireless devices sharing the same resources (e.g. common or adjacent bands of frequencies) or an ad-hoc network.

Consider now a given transmitter-receptor (transmitter-receiver) pair. The power at the Rx antenna output  $P_r$  coming from the transmitter is given by the standard link budget equation [6],

$$P_r = P_t G_t G_r g \quad (2)$$

where  $P_t$  is the Tx power,  $G_t, G_r$  are the Tx and Rx antenna gains, and  $g$  is the propagation path gain ( $=1/\text{path loss}$ ),  $g = g_a g_l g_s$ , where  $g_a$  is the average propagation path gain, and  $g_l, g_s$  are the contributions of large-scale (shadowing) and small-scale (multipath) fading, which can be modeled as independent log-normal and Rayleigh (Rice) random variables, respectively [6].

The widely-accepted model for  $g_a$  is  $g_a = a_\nu R^{-\nu}$ , where  $\nu$  is the path loss exponent, and  $a_\nu$  is constant independent of  $R$  [6]. In the traditional link-budget analysis of a point-to-point link, it is a deterministic constant. However, in our network-level model  $g_a$  becomes a random variable since the Tx-Rx distance  $R$  is random (due to random location of the nodes) and it is this random variable that represents a new type of fading, which we term “network-scale fading”, since it exhibits itself on the scale of the whole area occupied by the network. Since  $g_a$  does not depend on the local propagation

environment around the Tx or Rx ends that affect  $g_l, g_s$  but only on the global configuration of the Tx-Rx propagation path (including the distance  $R$ , of which  $g_l, g_s$  are independent) [6], the network-scale fading in this model is independent of the large-scale and small-scale ones, which is ultimately due to different physical mechanisms generating them. The distribution functions of  $g_a$  in various scenarios have been given in [8]-[10].

### III. PDF OF INTERFERENCE LEVELS AND THE INTERFERENCE TO NOISE RATIO

We consider a fixed-position receptor and a number of randomly located interfering transmitters (interferers, e.g. mobile units of other users) of the same power  $P_t$  (following the framework in [7]-[10], this can also be generalized to the case of unequal Tx powers). Only the network-scale fading is taken into account in this section, assuming that  $g_l = g_s = 1$  (this assumption is relaxed in section 4). For simplicity, we also assume that the Tx and Rx antennas are isotropic (this assumption is relaxed below), and consider the interfering signals at the receiver input.

The statistics of transmitters' location is given by (1). Transmitter  $i$  produces the average power  $P_{ai} = P_t g_a(R_i)$  at the receiver input, and we consider only the signals exceeding the Rx noise level  $P_0$ ,  $P_{ai} \geq P_0$ . We define the interference-to-noise ratio (INR)  $d_a$  in the ensemble of the interfering signals via the most powerful (at the Rx input) signal (It can be shown that, in the small outage region, the total interference power (i.e. coming from all transmitters) is dominated by the contribution of the most powerful signal, i.e. the single events dominate the outage probability [11]),

$$d_a = P_{a1} / P_0 \quad (3)$$

where, without loss of generality, we index the transmitters in the order of decreasing Rx power,  $P_{a1} \geq P_{a2} \geq \dots \geq P_{aN}$ . The most powerful signal is coming from the transmitter located at the minimum distance  $r_1$ ,  $P_{a1} = P_t g_a(r_1)$ . The cumulative distribution function (CDF) of the minimum distance can be easily found [7]-[9],

$$F_1(r) = 1 - \exp(-\bar{N}(V)), \quad \bar{N}(V) = \int_V \rho dV, \quad (4)$$

where  $\bar{N}(V)$  is the average number of transmitters in the ball  $V(r)$  of radius  $r$ . The corresponding PDF can be found by differentiation,

$$f_1(r) = e^{-\bar{N}} \int_{V'(r)} \rho dV \quad (5)$$

where  $V'(r)$  is sphere of radius  $r$  and the integral in (5) is over this sphere.

The probability that the INR exceeds value  $D$  is

$\Pr\{d_a > D\} = \Pr\{r_1 < r(D)\} = F_1(r(D))$ , where  $r(D)$  is such that  $P_a(r(D)) = P_0 D$ , so that the CDF of  $d_a$  is

$$F_d(D) = 1 - \Pr\{d_a > D\} = \exp(-\bar{N}(D)) \quad (6)$$

where  $\bar{N}(D)$  is the average number of transmitters in the ball  $V(r(D))$  of the radius  $r(D) = (P_t a_v / P_0 D)^{1/\nu}$ . The corresponding PDF can be obtained by differentiation,

$$f_d(D) = \frac{r(D) e^{-\bar{N}(D)}}{\nu D} \int_{V'(r(D))} \rho dV \quad (7)$$

When the average spatial density of transmitters is constant,  $\rho = const$ , (6), (7) simplify to [7]-[10],

$$F_d(D) = \exp\left\{-c_m \rho \left(\frac{P_t a_v}{P_0 D}\right)^{m/\nu}\right\} = \exp\left\{-\bar{N}_{\max} D^{-m/\nu}\right\},$$

$$f_d(D) = \frac{m}{\nu} \bar{N}_{\max} D^{-m/\nu-1} \exp\left\{-\bar{N}_{\max} D^{-m/\nu}\right\} \quad (8)$$

where  $c_1 = 2$ ,  $c_2 = \pi$  and  $c_3 = 4\pi/3$ ,  $\bar{N}_{\max} = c_m R_{\max}^m \rho$  is the average number of transmitters in the ball of radius  $R_{\max}$ , which we term "potential interference zone", and  $R_{\max}$  is such that  $P_a(R_{\max}) = P_0$ , i.e. a transmitter at the boundary of the potential interference zone produces signal at the receiver exactly at the noise level; transmitters located outside of this zone produce weaker signals, which are neglected in the analysis. Note that (8) gives the distribution of the INR as a simple explicit function of the system and geometrical parameters, and ultimately depends on  $\bar{N}_{\max}, m, \nu$  only.

When  $(k-1)$  most powerful signals, which are coming from  $(k-1)$  closest transmitters, do not create any interference (i.e. due to frequency, time or code separation in the multiple access scheme, or due to any other form of separation or filtering), the CDF and PDF of the distance  $r_k$  to the most powerful interfering signal of order  $k$  can be found in a similar way. The CDF of the INR  $d_a$  in this case is given by

$$F_{dk}(D) = e^{-\bar{N}(D)} \sum_{i=0}^{k-1} \bar{N}(D)^i / i! \quad (9)$$

In the case of constant average density  $\rho = const$ , the CDF and PDF of the INR simplify to [7]-[10],

$$F_{dk}(D) = \exp\left\{-\bar{N}_{\max} D^{-m/\nu}\right\} \sum_{i=0}^{k-1} \frac{1}{i!} \left(\frac{\bar{N}_{\max}}{D^{m/\nu}}\right)^i,$$

$$f_{dk}(D) = \frac{m}{v} \frac{\bar{N}_{\max}^k}{(k-1)!} D^{-\frac{km}{v}-1} \exp\{-\bar{N}_{\max} D^{-m/v}\} \quad (10)$$

which are also explicit functions of  $\bar{N}_{\max}, m, v$ .

On the other hand, the PDF of interference power  $P_a$  coming from a single, randomly-selected node located in the potential interference zone is, for  $\rho = \text{const}$ , [7]-[10]:

$$f_a(P_a) = \frac{m P_0^{m/v}}{v P_a^{(m+v)/v}}, \quad P_a \geq P_0 \quad (11)$$

Using this, (10) can be derived as well by analysing the max/min ratio for an ensemble of interfering signals, each having the PDF in (11). Note that this PDF does not have 1<sup>st</sup> and 2<sup>nd</sup> moments for some important values of  $m$  and  $v$  (because of its “long” tail, e.g.  $m=2, v=2$  (planar distribution and free-space propagation). Another interesting property of (11) is that it is independent of the Tx power and node density and depends on only three basic parameters ( $m, v, P_0$ ), so that nodes with different powers and densities as well as their combinations (e.g. a non-homogeneous network) will induce the same distribution. The same applies to the case of random Tx power (including fading channels). Unfortunately, this conclusion does not extend to (10) (see [11] for a detailed analysis of the impact of fading in this case).

#### IV. OUTAGE PROBABILITY-NODE DENSITY TRADEOFF

Powerful interfering signals can result in significant performance degradation due to linear and nonlinear distortion effects in the receiver when they exceed certain limit, which we characterize here via the receiver distortion-free dynamic range (i.e. the maximum acceptable interference-to-noise ratio)  $D_{df} = P_{\max}/P_0$ , where  $P_{\max}$  is the maximum interfering signal power at the receiver that does not cause significant performance degradation. If  $d_a > D_{df}$ , there is significant performance degradation and the receiver is considered to be in outage, which corresponds to one or more transmitters falling into the active interference zone (i.e. the ball of radius  $r(D_{df})$ ); the signal power coming from transmitters at that zone exceeds  $P_{\max}$ , whose probability is

$$\mathcal{P}_{out} = \Pr\{d_a > D_{df}\} = 1 - F_d(D_{df}) \quad (12)$$

For given  $\mathcal{P}_{out}$ , one can find the required distortion-free dynamic range (“outage dynamic range”)  $D_{df}$

$$D_{df} = F_d^{-1}(1 - \mathcal{P}_{out}) \quad (13)$$

We note that, in general,  $D_{df}$  is a decreasing function of  $\mathcal{P}_{out}$ , i.e. low outage probability calls for high distortion-free dynamic range. For simplicity of notations, we further drop

the subscript and denote the spurious-free dynamic range by  $D$ .

##### A. All interfering signals are active ( $k=1$ ):

We consider first the case of  $k=1$ , i.e. all interfering signals are active. The outage probability can be evaluated using (6) and (12). From practical perspective, we are interested in the range of small outage probabilities  $\mathcal{P}_{out} \ll 1$ , i.e. high-reliability and communications. When this is the case,  $F_d(D) \rightarrow 1$  and using MacLaurean series expansion  $e^{-\bar{N}} \approx 1 - \bar{N}$ , (12) simplifies to

$$\mathcal{P}_{out} \approx \bar{N} = \int_{V(r(D))} \rho dV \quad (14)$$

which further simplifies, in the case of  $\rho = \text{const}$ , to

$$\mathcal{P}_{out} \approx \bar{N}_{\max} D^{-m/v} \quad (15)$$

Note that, in this case, the outage probability  $\mathcal{P}_{out}$  scales linearly with the average number  $\bar{N}_{\max}$  of nodes in the potential interference zone, and it effectively behaves as if the number of nodes were fixed (not random) and equal to  $\bar{N}_{\max}$ . Based on this, we conclude that the single-order events (i.e. when only one signal in the ensemble of interfering signals exceeds the threshold  $P_{\max}$ ) are dominant contributor to the outage. This immediately suggests a way to reduce significantly the outage probability by eliminating (e.g. by filtering) the dominant interferer in the ensemble. Using (15), the required spurious-free dynamic range of the receiver can be found for given outage probability,  $D \approx (\bar{N}_{\max} / \mathcal{P}_{out})^{v/m}$ . Note that higher values of  $v$  and lower values for  $m$  call for higher dynamic range. Intuitively, this can be explained by the fact that when the transmitter moves from the boundary of the potential interference zone (i.e.  $R = R_{\max}$ ,  $P_a(R) = P_0$ ) closer to the receiver ( $R \ll R_{\max}$ ), the power grows much faster when  $v$  is larger, so that closely-located transmitters produce much more interference (compared to those located close to the boundary) when  $v$  is large, which, combined with the uniform spatial density of the transmitters, explains the observed behavior. The effect of  $m$  can be explained in a similar way.

To validate the accuracy of approximation in (14), and also the expressions for the dynamic range PDF and CDF in the previous section, extensive Monte-Carlo (MC) simulations have been undertaken. Fig. 1 shows some of the representative results. Note good agreement between the analytical results (including the approximations) and the MC simulations. It can be also observed that the tails of the distributions decay much slower for the  $v=4$  case, which indicates higher probability of high-power interference in that case and, consequently, requires higher spurious-free dynamic range of the receiver, in complete agreement with the predictions of the analysis. Note also that the outage probability evaluated via the total interference power coincides with that evaluated via the

maximum interferer power, at the small outage region (this result has been rigorously proved in [11]).

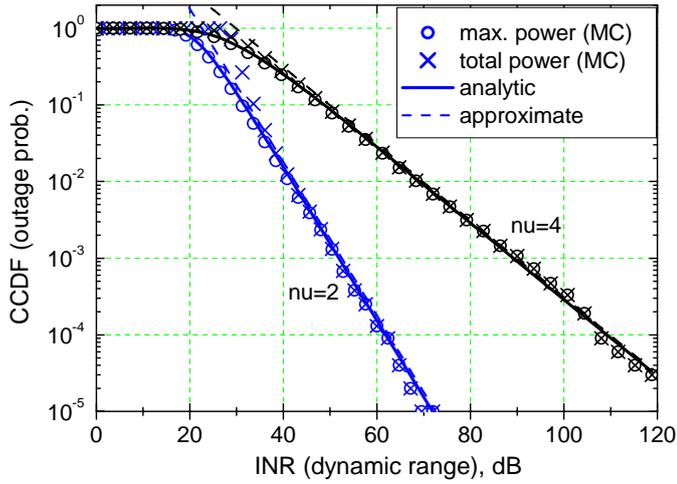


Figure 1. The CCDF of  $d_a = P_{a1}/P_0$  and  $d_{tot} = P_{tot}/P_0$  (also the outage probability) evaluated from Monte-Carlo (MC) simulations for  $m=2$ ,  $v=2&4$ ,  $P_0=10^{-10}$ ,  $P_t=1$ ,  $\rho=10^{-5}$ ; analytic CCDF of  $d_a$  (derived from (8)) and its approximation in (15) are also shown.

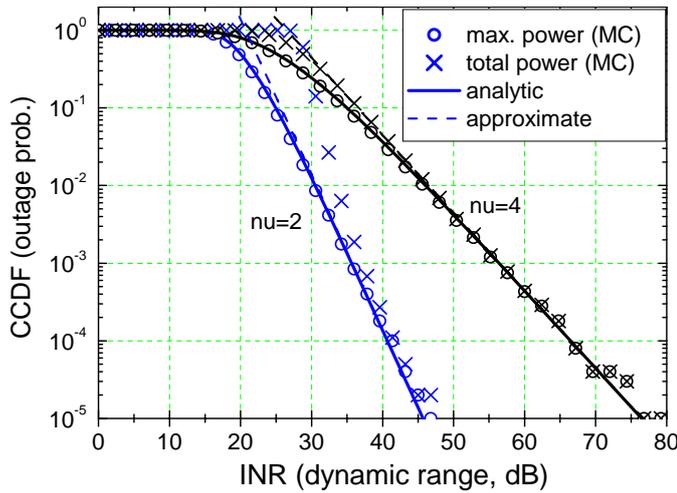


Figure 2. The CCDF of  $d_a = P_{a1}/P_0$  and  $d_{tot} = P_{tot}/P_0$  with the most powerful signal cancelled ( $k=2$ ), evaluated from MC simulations ( $10^5$  trials). Significant improvement due to interference cancellation for the whole range of INR (compare to Fig. 1) is clear.

Consider now a scenario where the actual outage probability has not to exceed a given value  $\mathcal{P}_{out}$  for the receiver with a given distortion-free dynamic range  $D$ . Using (8) and (12), the average number of transmitters in the active interference zone (ball of radius  $r(D)$ ) can be upper bounded as  $\bar{N} \leq -\ln(1 - \mathcal{P}_{out})$ . Using the expression for  $\bar{N}$ , one obtains a basic tradeoff relationship between the network density and the outage probability,

$$\bar{N} = \int_{V(r(D))} \rho dV \leq -\ln(1 - \mathcal{P}_{out}) \quad (16)$$

i.e. for given outage probability, the network density is upper bounded or, equivalently, for given network density, the outage probability is lower bounded.

In the case of uniform density  $\rho = const$  and small outage probability,  $\mathcal{P}_{out} \ll 1$ , this gives an explicit tradeoff relationship between the maximum distortion-free interference power at the receiver  $P_{max}$ , the transmitter power  $P_t$  and the average node density for distortion-free receiver operation,

$$\rho \leq c_m^{-1} \mathcal{P}_{out} (P_{max} / P_t a_v)^{m/v} \quad (17)$$

or, equivalently, an upper bound on the average density of nodes in the network. As intuitively expected, higher  $\mathcal{P}_{out}, P_{max}, v$  and lower  $P_t, m$  allow for higher network density. The effect of  $v$  is intuitively explained by the fact that higher  $v$  results in larger path loss or, equivalently, in smaller distance at the same path loss, so that the transmitters can be located more densely without increasing interference level. The effect of the other parameters can be explained in a similar way.

### B. $(k-1)$ strongest interfering signals are inactive:

We now assume that  $(k-1)$  strongest interfering signals are eliminated via some means (e.g. by filtering or resource allocation). In this case, (9), (10) apply and (14) generalizes to

$$\mathcal{P}_{out} \approx \frac{1}{k!} \bar{N}^k = \frac{1}{k!} (\bar{N}_{max} D^{-m/v})^k \quad (18)$$

which can be expressed as  $\mathcal{P}_{out} = \frac{1}{k!} \mathcal{P}_{out,1}^k \leq \mathcal{P}_{out,1}$ , where  $\mathcal{P}_{out,1}$  is the outage probability for  $k=1$  (see (14)). In the small outage region,  $\mathcal{P}_{out,1} \ll 1$  and  $\mathcal{P}_{out} \ll \mathcal{P}_{out,1}$ , i.e. there is a significant beneficial effect of removing  $(k-1)$  strongest interferers, which scales exponentially with  $k$ . Further comparison to the corresponding result in [5] shows that the assumption there of cancelling *all* interferers, which exceed the required signal and are in the disk with the given average number of interferers, affects significantly the result (no exponential scaling). It should also be noted that, contrary to the  $k=1$  case,  $\mathcal{P}_{out}$  in (18) is super-linear in  $\bar{N}_{max}$ : doubling  $\bar{N}_{max}$  increases  $\mathcal{P}_{out}$  by the factor  $2^k > 2$ , i.e.  $\mathcal{P}_{out}$  is more sensitive to  $\bar{N}_{max}$  in this case.

In a similar way, the node density-outage probability tradeoff can be formulated. In the for small outage probability region  $\mathcal{P}_{out} \ll 1$ , it can be expressed as

$$\bar{N} = \int_{V(r(D))} \rho dV \leq (k! \mathcal{P}_{out})^{1/k} \quad (19)$$

Comparing (19) to (16), one can clearly see the beneficial effect of “removing”  $(k-1)$  most powerful interferers on the outage probability-network density tradeoff, since

$(k!P_{out})^{1/k} \gg P_{out}$  in the small outage regime, so that higher node density is allowed at the same outage probability. It is illustrated by curves on Fig.2.

In the case of uniform density, (19) reduces to

$$\rho \leq c_m^{-1} (k!P_{out})^{1/k} (P_{max} / P_t a_v)^{m/v} \quad (20)$$

which is a generalization of (17) to  $k \geq 1$ .

### C. Impact of Rayleigh and log-normal fading:

Following the same approach as in [3], it can be shown that the impact of Rayleigh and log-normal fading on the distributions above is a shift by a constant factor. In the case of Rayleigh fading, the constant is close to 1 and, thus, can be neglected so that the distributions are roughly not affected. In the case of log-normal fading, the constant is not negligible. The intuition behind this result is that the distributions in (12), (15), (18) are much more heavily-tailed (slowly-decaying) than the Rayleigh distribution so that outage events in the combined distribution are mostly caused by nearby interferers without deep Rayleigh fades and the combined distribution is roughly the same as the original one (without fading). On the other hand, the log-normal distribution is also heavily-tailed, so it cannot be neglected (see [11] for a detailed analysis of the fading effects).

## V. OUTAGE PROBABILITY: MEASURE OF INDUCED ELECTROMAGNETIC ENVIRONMENTAL RISKS

As it was mentioned before, environmental risks induced by EME in wireless networks are determined by the level of dominant interference at the receptor allocation. The threshold values  $\Pi_{E1}-\Pi_{E4}$  of these levels in terms of the power flux density (PFD) of an electromagnetic field and used as an electromagnetic safety criteria, are given below [10].

TABLE 1. SOME CRITERIA OF ELECTROMAGNETIC SAFETY

PFD, $\mu\text{W}/\text{cm}^2$	Description
0,1 ( $\Pi_{E1}$ )	Preliminary preventive Maximum Permissible Level (MPL) for «total common electromagnetic irradiations from all high-frequency equipment with very low pulsing modulation» (recommended). Equal or close to the MPL accepted in some countries/regions.
1,0 ( $\Pi_{E2}$ )	Highest level of intensity of an electromagnetic background that is save for the population. Accepted earlier in the USSR up to 1984 as the MPL for the population
2,0 ( $\Pi_{E3}$ )	The MPL accepted in Moscow and Paris for places of round-the-clock stay of people
10,0 ( $\Pi_{E4}$ )	The MPL for the population, accepted in Russia, Belarus and also in a number of the European and Asian countries

The level  $\Pi_b$  [ $\text{W}/\text{m}^2$ ] of the receiver desensitization/blocking, determined at the antenna location,

exceeds the receiver sensitivity  $\Pi_{min}$  [ $\text{W}/\text{m}^2$ ] by the blocking dynamic range  $D_{dfb}$ :

$$\Pi_b = D_{dfb} \Pi_{min} \quad (21)$$

A comparison between the level of radio receiver desensitization/blocking and the levels in the electromagnetic safety criteria, for typical values of receiver sensitivity  $\Pi_{min}$  and the receiver dynamic range  $D_{dfb}$ , are given in Table 2.

TABLE 2.

$\Pi_{min}$ , $\text{W}/\text{m}^2$	$\Pi_b$ , $\mu\text{W}/\text{cm}^2$		
	$D_{dfb}=70\text{dB}$	$D_{dfb}=80\text{dB}$	$D_{dfb}=90\text{dB}$
$10^{-12}$	$10^{-3}$	$10^{-2}$	$\Pi_{E1}$
$10^{-11}$	$10^{-2}$	$\Pi_{E1}$	$\Pi_{E2}, \approx \Pi_{E3}$
$10^{-10}$	$\Pi_{E1}$	$\Pi_{E2}, \approx \Pi_{E3}$	$\Pi_{E4}$

Clearly, the levels of out-of-band interference causing desensitization for highly-linear receivers (high  $D_{dfb}$ ) roughly equal to the MPL levels required from the ecological point of view, which is an indication of close similarity of EMC and EMS problems in wireless communications.

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